

Lecture 10  
Phase Diagrams:  
Development of Microstructure  
and Alteration of Mechanical  
Properties



# The Kinetics of Phase Transformations

- Process of phase transformation occurs in two stages:
  - Nucleation
    - The initial stage in a phase transformation. It is evidenced by the formation of small particles of the new phase that can grow.
  - Growth
    - During a phase transformation and after nucleation, the increase in size of a particle of a new phase.



# The Kinetics of Phase Transformations

- Nucleation
  - Two types: Homogeneous and Heterogeneous
    - Homogeneous
      - Nuclei appear uniformly
    - Heterogeneous
      - Nuclei can appear in insoluble impurities, grain boundaries and dislocations.



# The Kinetics of Phase Transformations

- Homogenous Nucleation

- Free energy – defined in lecture 9.

- We care about the change in Gibbs free energy  $\Delta G$ . A negative value of  $\Delta G$  means a transformation can occur.

- Consider solidification of a pure material

- Assume spherical shape to nuclei of radius  $r$ .

- $\Delta G$  = volume free energy + surface free energy

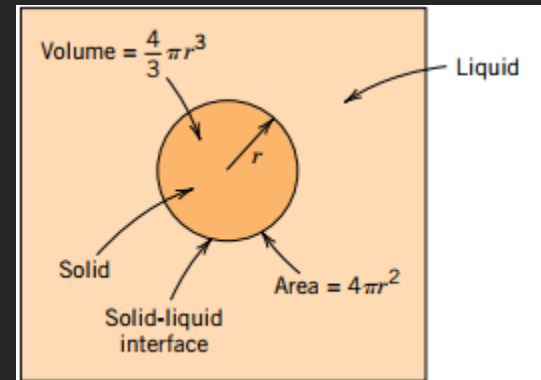
- $\Delta G = \frac{4}{3}\pi r^3 \Delta G_v + 4\pi r^2 \gamma$

- Critical radius  $r^* = -\frac{2\gamma}{\Delta G_v}$

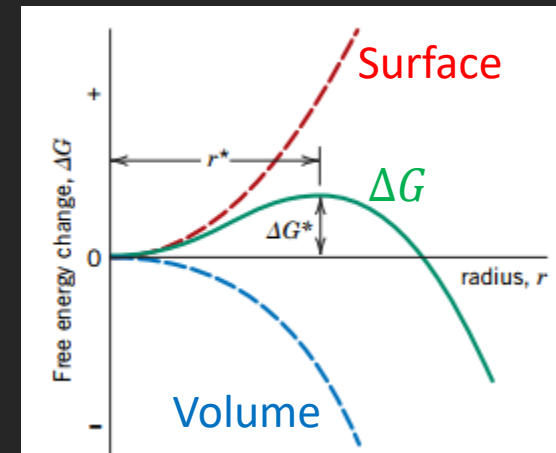
- Corresponds to  $G_v^* = \frac{16\pi\gamma^3}{3(\Delta G_v)^2}$ , which is the activation energy to form a stable nuclei

- $\Delta G_v = \Delta H_f \frac{(T_m - T)}{T_m}$ , where  $\Delta H_f$  is the latent heat of fusion and  $T_m$  is the equilibrium solidification temperature in Kelvin.

- As temperature decreases, so does the critical radius and Gibbs energy becomes more negative.



**Figure 10.1** Schematic diagram showing the nucleation of a spherical solid particle in a liquid.



# The Kinetics of Phase Transformations

- Homogenous Nucleation

- Number of stable nuclei expressed by an Arrhenius equation

$$n^* = K_1 \cdot e^{-\frac{\Delta G^*}{k_b T}}$$

- Diffusion also plays a role:

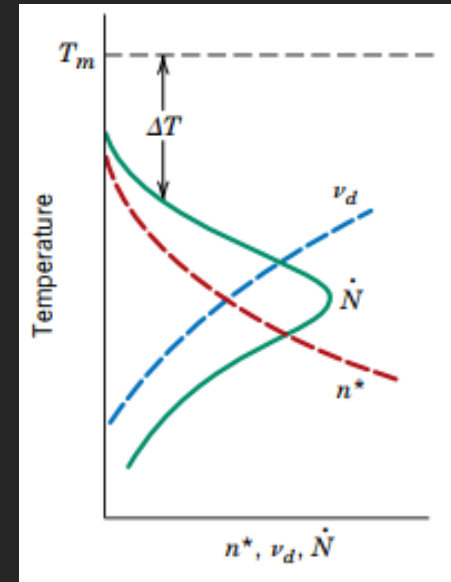
$$v_d = K_2 e^{-\frac{Q_d}{RT}}$$

- $Q_d$  activation energy for diffusion
- $K_2$  is a constant

- Nucleation rate expression for homogenous nucleation

$$\dot{N} = K_3 n^* v_d$$

- $K_3$  is the number of atoms on a nucleus surface.



# The Kinetics of Phase Transformations

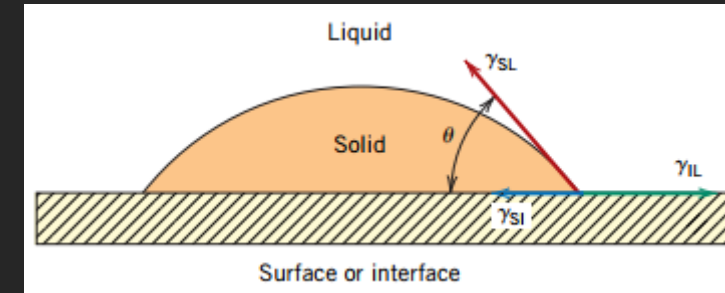
- Heterogeneous Nucleation

- Its easier for nucleation to occur preexisting surfaces and interfaces.
- Consider nucleation on a flat surface
  - $\gamma_{IL} = \gamma_{SI} + \gamma_{SL} \cos(\theta)$
- Critical radius and activation energy for heterogenous nucleation

$$r^* = -\frac{2\gamma_{SL}}{\Delta G_v}$$

$$\Delta G^* = \left( \frac{16\pi\gamma_{SL}^3}{3\Delta G_v^2} \right) S(\theta)$$

- $\Delta G_{het}^* = \Delta G_{homo}^* S(\theta)$ , where  $S(\theta)$  ranges from 0 to 1.



**Figure 10.5** Heterogeneous nucleation of a solid from a liquid. The solid–surface ( $\gamma_{SI}$ ), solid–liquid ( $\gamma_{SL}$ ), and liquid–surface ( $\gamma_{IL}$ ), interfacial energies are represented by vectors. The wetting angle ( $\theta$ ) is also shown.



# The Kinetics of Phase Transformations

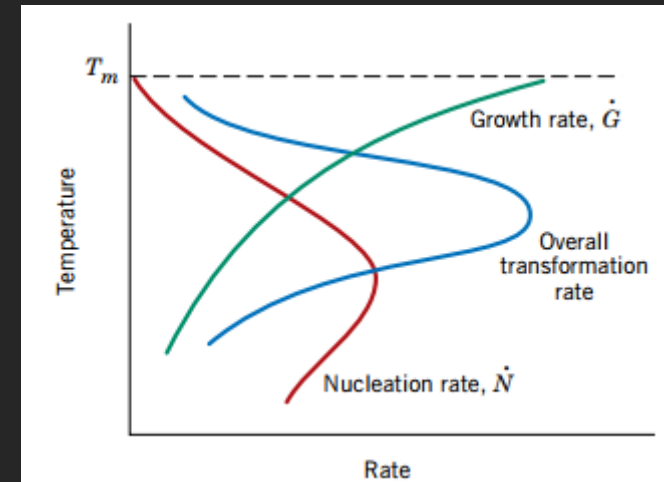
- Growth

- This stage begins when  $r_{embryo} > r^*$
- Growth rate

$$\dot{G} = C e^{-\frac{Q}{k_b T}}$$

- The overall rate of transformation is some product of the growth rate and nucleation rate.

- Transformations happening at temperatures close to equilibrium temperature correspond to low nucleation and high growth rate, leading to few but large grains.
- Inversely proportional to time required for some degree of completion.



**Figure 10.8** Schematic plot showing curves for nucleation rate ( $\dot{N}$ ), growth rate ( $\dot{G}$ ), and overall transformation rate versus temperature.



# The Kinetics of Phase Transformations

- Kinetic Considerations of Solid-State Transformations

- Kinetics

- The study of reaction rates and the factors that affect them

- Avrami Equation

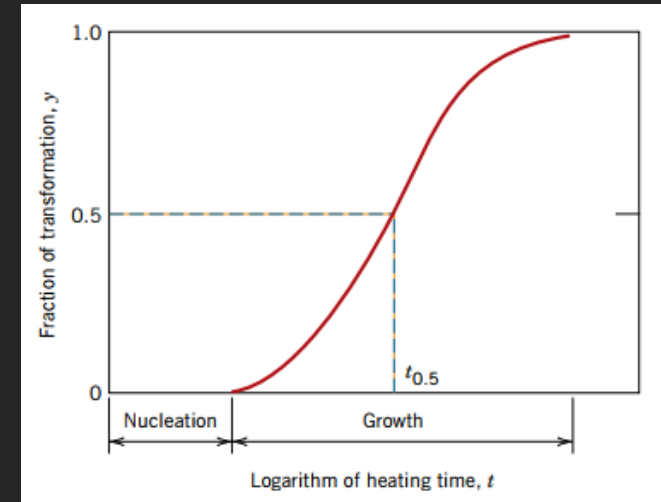
- Dependence of fraction of transformation on time.

- $y = 1 - e^{-kt^n}$

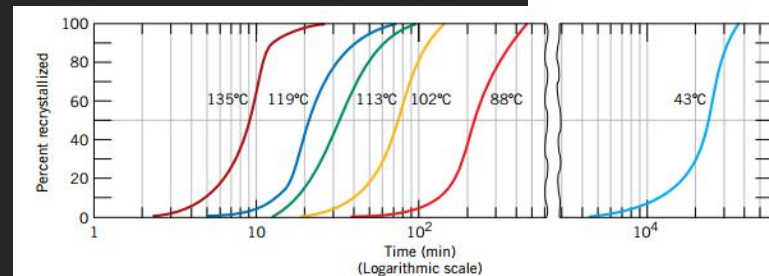
- $k$  and  $n$  are constants for the reaction.

- The rate of transformation is

$$rate = \frac{1}{t_{0.5}}$$



**Figure 10.10** Plot of fraction reacted versus the logarithm of time typical of many solid-state transformations in which temperature is held constant.



**Figure 10.11** Percent recrystallization as a function of time and at constant temperature for pure copper. (Reprinted with permission from *Metallurgical Transactions*, Vol. 188, 1950, a publication of The Metallurgical Society of AIME, Warrendale, PA. Adapted from B. F. Decker and D. Harker, "Recrystallization in Rolled Copper," *Trans. AIME*, 188, 1950, p. 888.)

# Microstructural and Property changes in Iron-Carbon Alloys

- Isothermal Transformation Diagrams

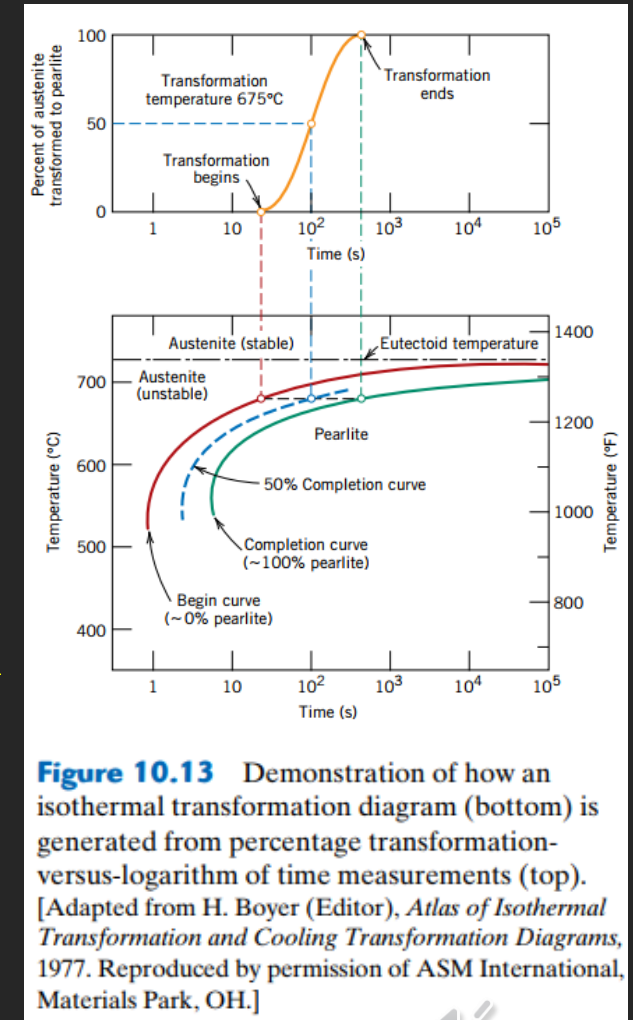
- Pearlite

- Eutectoid reaction for the iron-iron carbide system fundamental to the development of microstructure in steel alloys.



- Isothermal Transformation diagrams (T-T-T plots)

- A plot of temperature versus the logarithm of time for a steel alloy of definite composition. Used to determine when transformations begin and end of an isothermal heat treatment of a previously austenitized alloy.
    - Different compositions will have different TTT plots.

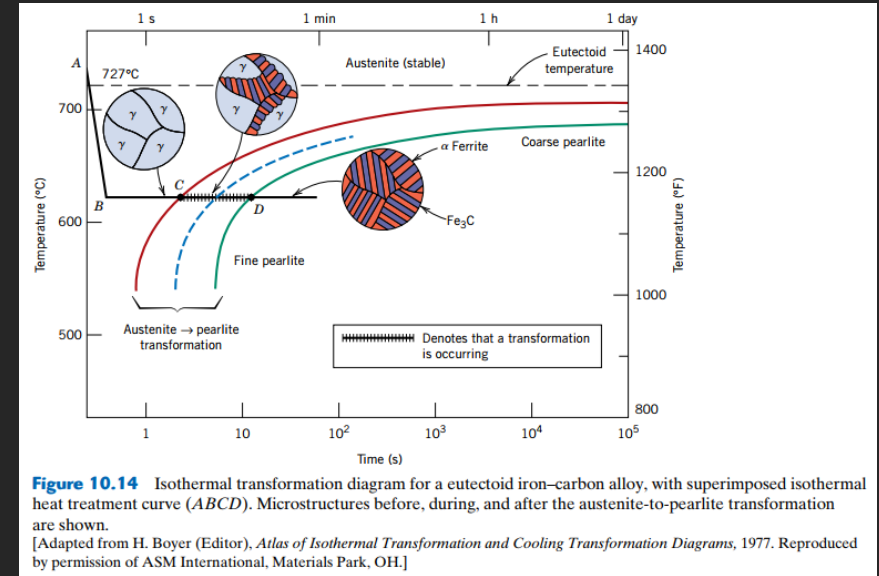


**Figure 10.13** Demonstration of how an isothermal transformation diagram (bottom) is generated from percentage transformation-versus-logarithm of time measurements (top). [Adapted from H. Boyer (Editor), *Atlas of Isothermal Transformation and Cooling Transformation Diagrams*, 1977. Reproduced by permission of ASM International, Materials Park, OH.]



# Microstructural and Property changes in Iron-Carbon Alloys

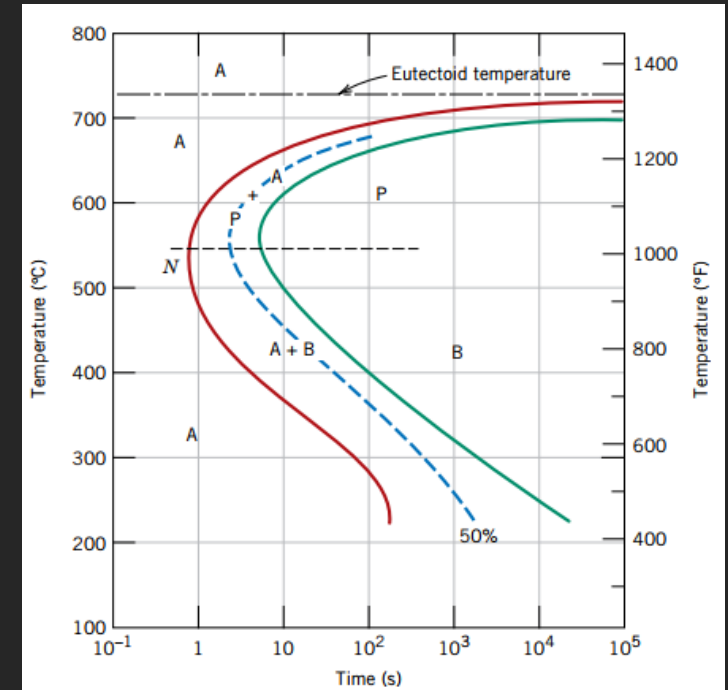
- Isothermal Transformation Diagrams
  - Pearlite
  - Isothermal Transformation diagrams (T-T-T plots)
    - Line A-B: Rapid cooling
    - Isothermal treatment at line BCD
    - Coarse Pearlite
      - Pearlite for which the alternating ferrite and cementite layers are thick
    - Fine Pearlite
      - Pearlite I which the alternating ferrite and cementite layers are relatively thin.



# Microstructural and Property changes in Iron-Carbon Alloys

## • Bainite

- An austenitic transformation product found in some steel and cast irons. It forms at temperatures between those at which pearlite and martensite transformations occur. The microstructure consists of a  $\alpha$ -ferrite and a fine dispersion of cementite.
- Cannot transform pearlite  $\leftrightarrow$  bainite without first heating back up to Austenite.



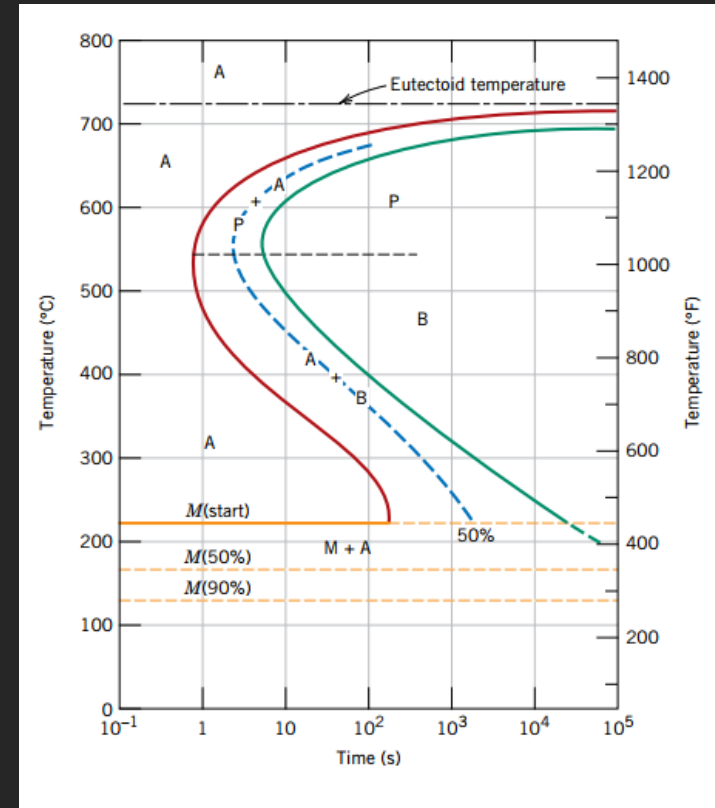
**Figure 10.18** Isothermal transformation diagram for an iron-carbon alloy of eutectoid composition, including austenite-to-pearlite (A-P) and austenite-to-bainite (A-B) transformations.

[Adapted from H. Boyer (Editor), *Atlas of Isothermal Transformation and Cooling Transformation Diagrams*, 1977. Reproduced by permission of ASM International, Materials Park, OH.]

# Microstructural and Property changes in Iron-Carbon Alloys

- **Martensite**

- A metastable iron phase supersaturated in carbon that is the product of diffusionless (athermal) transformation.
- Happens when rapidly cooled and prevents carbon diffusion.
- FCC austenite transform to BCT martensite.
- Time independent transformation- instantaneous
  - Non-equilibrium phase. Does not show up in iron-iron carbide phase diagram.

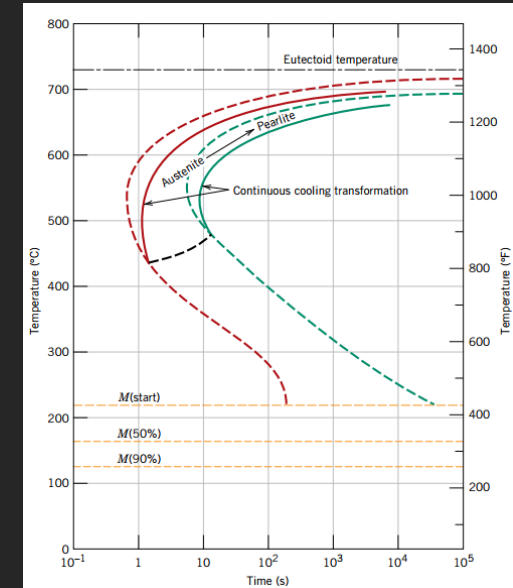


**Figure 10.22** The complete isothermal transformation diagram for an iron-carbon alloy of eutectoid composition: A, austenite; B, bainite; M, martensite; P, pearlite.



# Microstructural and Property changes in Iron-Carbon Alloys

- Continuous-Cooling Transformation Diagrams (CCT)
  - A plot of temperature versus the logarithm of time for a steel alloy. Used to indicate when transformations occur as the initially austenitized material is continuously cooled at a specified rate; in addition, the final microstructure and mechanical characteristics may be predicted.



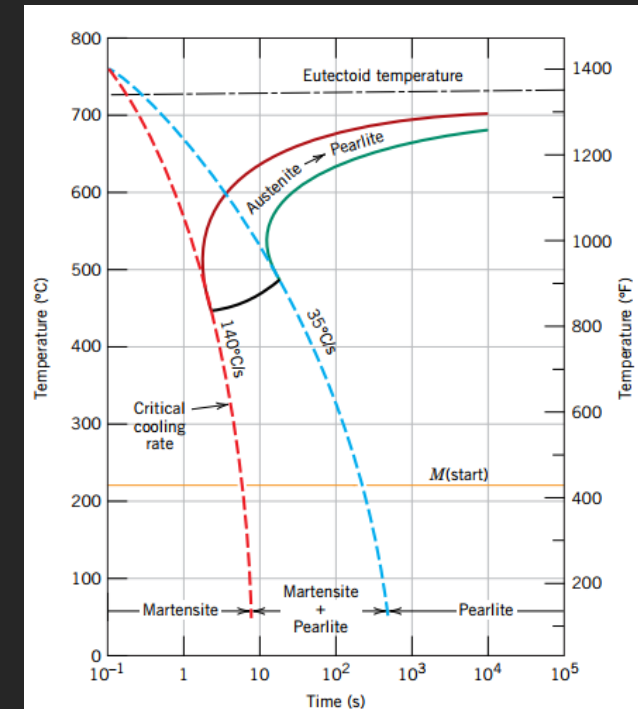
**Figure 10.25** Superimposition of isothermal and continuous-cooling transformation diagrams for a eutectoid iron-carbon alloy.

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# Microstructural and Property changes in Iron-Carbon Alloys

- Continuous-Cooling Transformation Diagrams (CCT)
  - Most cases, all austenite transforms to pearlite before any bainite shows up when continuously cooling.
  - There are critical cooling rates that can help determine of the cooled product will be all martensite, pearlite or the combination of the two.
- CCTs and TTT plots can be seen as phase diagrams with a time component.



**Figure 10.27** Continuous-cooling transformation diagram for a eutectoid iron-carbon alloy and superimposed cooling curves, demonstrating the dependence of the final microstructure on the transformations that occur during cooling.

